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**TECHNICAL REPORT BRL-TR-2846** 

## INJECTION PROCESSES IN LIQUID REGENERATIVE PROPELLANT GUNS

TERENCE P. COFFEE

**AUGUST 1987** 

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US ARMY BALLISTIC RESEARCH LABORATORY ABERDEEN PROVING GROUND, MARYLAND



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In a previous report, I discussed the analysis of experimental measurements for a 30mm regenerative liquid propellant gun. Discharge coefficients for the injection into the combustion chamber and values for the Sauter mean diameter of droplets in the combustion chamber were derived. More recently, pressure measurements were also taken in the gun tube. This allows the derivation of discharge coefficients for the flow into the tube. A number of improvements have been made in the inverse analysis. Also, work has been done in developing a transient model to predict the discharge coefficients into the combustion chamber.						
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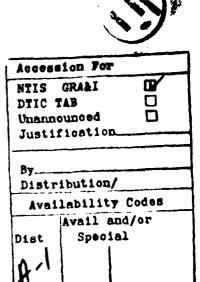
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#### I. INTRODUCTION

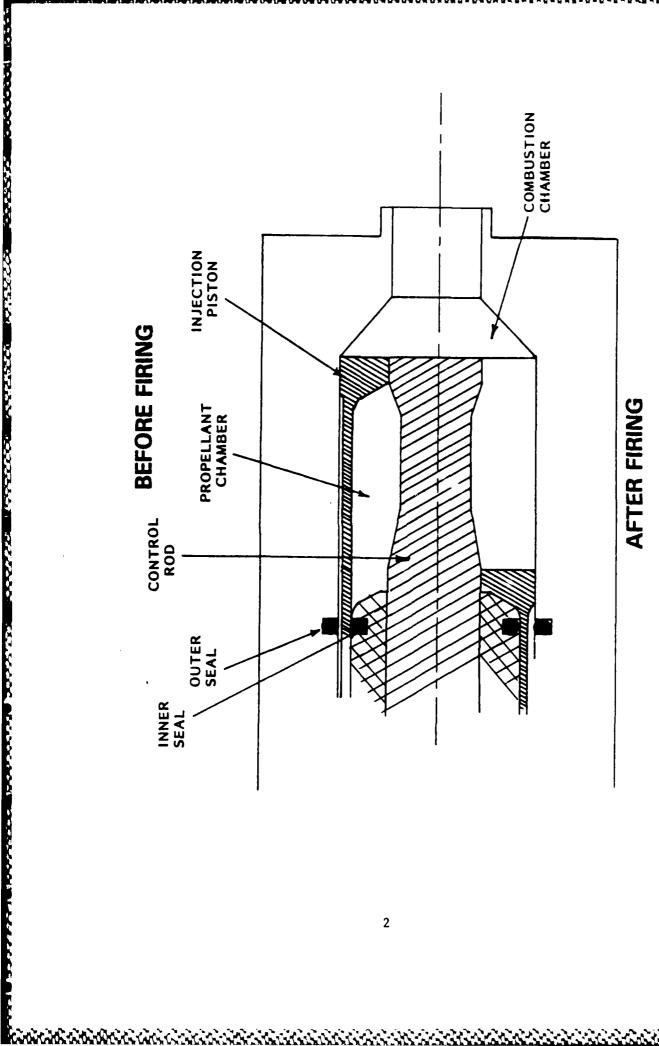
In this article we consider annular liquid propellant guns (see Figure 1). The regenerative piston surrounds a central rod. As the piston begins to move, it opens up a small annular vent between the piston and the bolt. The bolt is tapered, so the vent opening becomes gradually larger. There is a long straight section where the vent area is constant, and finally a back taper to slow down the piston.

The transducer block (crosshatched area) is mounted on Belleville springs (not shown). A set of pins, going through a spacer, actually connect the block and the springs. When the piston begins to move, it pushes back the liquid and the transducer block. Eventually, the block hits against the spacer. Very little injection takes place before the transducer block stops moving. The springs allow the piston to move past the O-ring and over the front taper in the bolt.

The liquid jet then enters the combustion chamber at high speed. The jet may stay in contact with the center bolt or separate from it. After some delay, the jet breaks up into droplets. The droplets formed may break up further or coalese. The propellant will eventually ignite, and may burn as individual droplets or as an envelope flame. Gas recirculation will further affect the spray combustion. It is possible that the time scale is too short for droplets to form, and the jet may form slugs of liquid or other irregular shapes. Also, there is a crash ring immediately in front of the center bolt. This will effect how the jet breaks up and combusts.

The fluid flows from the combustion chamber into the gun tube. For liquid guns, there is typically a large area change between the chamber and the tube.

Regenerative liquid propellant gun codes<sup>2-5</sup> involve a number of simplifying assumptions. As the codes consider only lumped parameter or at most one-dimensional regions, higher dimensional effects are ignored. Besides this, there are three major areas of uncertainty. First is the injection of the liquid propellant through the piston into the combustion chamber. This is



A Regenerative Liquid Propellant Gun with an Annular Piston Figure 1.

approximated as steady state Bernoulli flow. The various possible loss terms (entrance losses, frictional losses, inertial effects, etc.) are lumped into the discharge coefficient. This is treated as an adjustable parameter, and varied so as to obtain the desired chamber pressure.

Second is the liquid accumulation in the combustion chamber. For lack of further information, we usually assume that the liquid combusts instantaneously when it enters the combustion chamber, although simple droplet burning models are also available.

Last, there is the fluid flow from the combustion chamber into the gun tube. This flow is approximated by steady state Bernoulli or isentropic flow, again with an adjustable discharge coefficient to take into account unknown loss terms. This coefficient is normally set equal to one.

At the BRL we have a 30mm regenerative liquid propellant gun. A set of experimental measurements has been made on this fixture. These include the liquid reservoir pressure, the combustion chamber pressure, the piston travel, and the projectile velocity. More recent firings include three pressure measurements in the gun tube (3.81, 50.80, and 241.30 cm. downbore). The pressure traces have been filtered to remove the acoustic oscillations. A number of cases have been measured for the 2/3 charge (about 230 g) and the 1/3 charge. The gun has not yet been fired with a full charge.

The reproducibility of the 1/3 charge firings is not good, so this data is not considered here. We do not have any 2/3 charge cases where all the data was recorded successfully. In this article we consider the data from round 8, where the muzzle pressures were not recorded, and round 53, where the liquid pressure was not successfully recorded. Our goal is to obtain information about the three processes discussed above.

#### II. NOTATION

In this article, A represents area, E energy, e internal energy, M mass, p pressure, T temperature, V volume, and v velocity. Subscript 1 represents

the liquid reservoir, 3 the combustion chamber, and 4 the gun tube. Region 2 (intermediate chamber) does not exist for this fixture. A subscript L represents a liquid property, and a subscript G a gas property. For a complete description, see the List of Symbols.

#### III. DESCRIPTION OF THE TEXT FIXTURE

Working from the engineering drawings, I have made a scale model drawing of the liquid reservoir (see Figure ?). The combustion chamber side of the piston and bolt have been slightly simplified. The reservoir is initially sealed by an O-ring.

According to the drawings, the transducer block should initially be exactly at the end of the back taper. However, when the test fixture is assembled, the block is observed to be about 1/8 of an inch in front of this point. So the piston stroke, instead of the designed 6.8 cm., is about 6.4 cm. The computed propellant mass is 232 g. A measurement of the propellant needed to fill the reservoir gives a value of 227 g., which is reasonable agreement.

Another measurement<sup>8</sup> shows that the block can move back about 0.5 cm. before hitting a spacer. When the block stops moving, the momentum of the piston causes a rapid pressure rise in the liquid. However, this is observed to occur after the piston has moved approximately 0.6 cm. So I assume that as the block moves back the 0.5 cm, the piston moves 0.6 cm. This causes a small amount of liquid to be injected into the chamber. Figure 3 shows the reservoir after the block has bottomed out. The piston has cleared the 0-ring and is over the beginning of the front taper.

The volume of the combustion chamber may be computed. However, a crash ring is inserted into the chamber to protect against damage to the fixture if the piston reverses. This crash ring is complex in shape. So I use a measured value of 95 cc as the initial chamber volume. For the lumped parameter modeling, the volume is the only quantity required. The shape of the combustion chamber is irrelevant.

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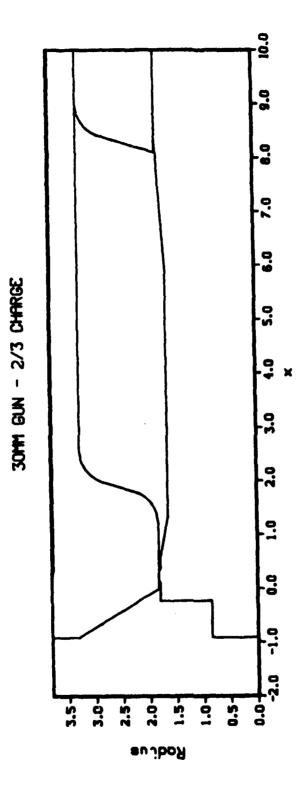
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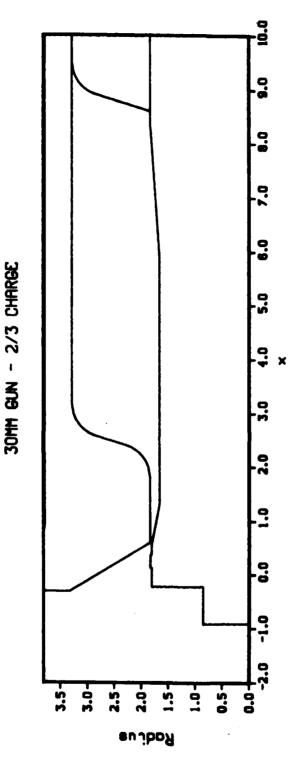
Another measurement shows that the block can move back about 0.5 cm. before hitting a spacer. When the block stops moving, the momentum of the piston causes a rapid pressure rise in the liquid. However, this is observed to occur after the piston has moved approximately 0.6 cm. So I assume that as the block moves back the 0.5 cm, the piston moves 0.6 cm. This causes a small amount of liquid to be injected into the chamber. Figure 3 shows the reservoir after the block has bottomed out. The piston has cleared the 0-ring and is over the beginning of the front taper.

The volume of the combustion chamber may be computed. However, a crash ring is inserted into the chamber to protect against damage to the fixture if the piston reverses. This crash ring is complex in shape. So I use a measured value of 95 cc as the initial chamber volume. For the lumped parameter modeling, the volume is the only quantity required. The shape of the combustion chamber is irrelevant.



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Scale Model Drawing of the Liquid Reservoir (Initial position) Figure 2.



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Figure 3. Scale Model Drawing of the Liquid Reservoir (After End of Block Motion)

There is a grease dyke between the piston and the wall of the chamber (except at the front) that helps support the piston. The pressure in the grease is only slightly higher than the combustion chamber pressure during the firing cycle. So in computing the hydraulic difference (combustion side area over liquid side area) the grease area is not included.

Other important numerical values are given in Table 1. Terms are defined in the List of Symbols.

TABLE 1. Fixture measurement.

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The liquid reservoir is pre-pressurized to 7.0 MPa. The primer will pressurize the combustion chamber to about 17 MPa. I do not attempt to model the details of the primer combustion.

## IV. PROPELLANT

The propellant used is HAN1846. The relevant properties are given in Table 2.

TABLE 2.

Property	Reference
ρ <sub>0</sub> = 1.43	9
e <sub>1</sub> = 4035.5	9
γ = 1.2226	9
c <sub>v</sub> = 1.6348	9
c <sub>p</sub> = 1.9987	9
b = .667	9
κ <sub>1</sub> = 5350.	10
K <sub>2</sub> = 9.11	10
A = 1.64	11
B = .103	11

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The equation of state of the liquid is derived assuming that the fluid is isothermal. The result is

$$\rho_{L} = \rho_{o} \left[ \frac{\kappa_{2}}{\kappa_{1}} p + 1 \right]^{1/\kappa_{2}}$$
 (1)

The linear burning rate was measured for a gelled propellant for pressures less than 100 MPa. The form of the equation is

linear burning rate = 
$$Ap^B$$
 (2)

There is some evidence that there is a break in the burning rate expression around 100 MPa, and that the exponent becomes much larger. For this paper, I will simply extrapolate the measured rate.

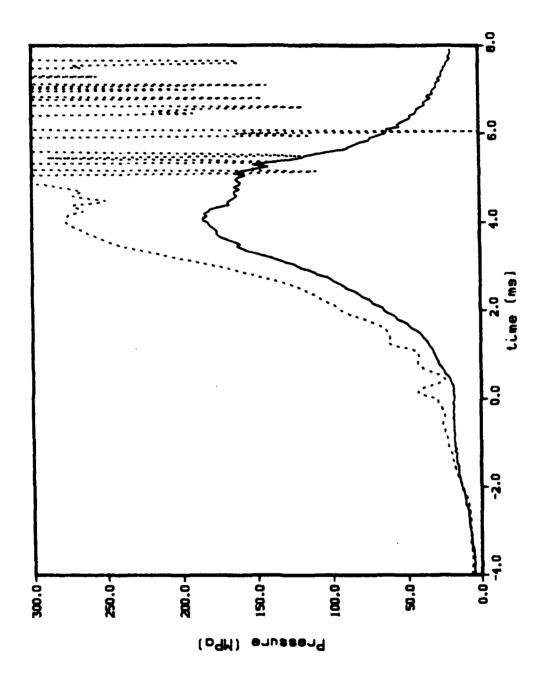
#### V. EXPERIMENTAL DATA

Figure 4 shows the measured chamber pressure and liquid pressure for round 8. All the data considered has been filtered to remove the high frequency oscillations. The time zero is taken to be the point where the Belleville springs bottom out.

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The igniter raises the pressure in the combustion chamber. This moves back the piston, the liquid, and the transducer block. The liquid pressure rises very slowly. At time zero, the block hits, and the momentum of the piston compresses the suddenly trapped liquid. Since the liquid is nearly incompressible, a small volume change leads to a large pressure change. This large pressure accelerates the liquid, and injection causes to pressure to undershoot. The liquid pressure oscillations gradually die out. As the piston nears the end of its stroke, the pressure measurement breaks up.

The piston travel is also measured (Figure 5). I am assuming that the first 0.5 cm of piston travel correspond to the block motion. The last 6.4 cm (taken to be positive) comprise the actual injection stroke. The velocity of the piston will also be required. In the previous paper, I used a finite difference approximation to obtain the velocity. The time difference had to be fairly large because of the noise in the signal. This lead to a loss of resolution. In this paper I fit the data by a parabolic spline. After some



Experimental Chamber Pressure (line) and Liquid Reservoir Pressure (dot); Round 8 Figure 4.

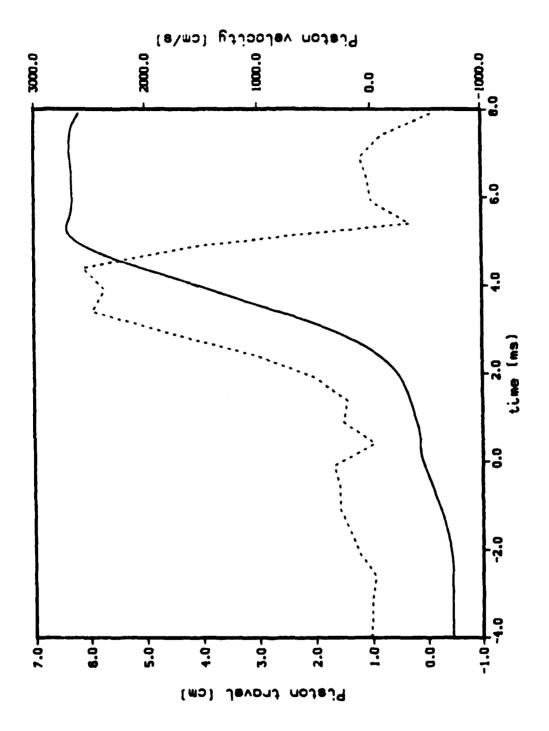


Figure 5. Experimental Piston Travel (line) and Derived Piston Velocity (dot); Round 8

experimentation, I used one parabola for each 0.5 ms. The parabolas are joined at the knots so that the entire curve is continuous and smooth. First and second time derivatives can be taken analytically. Figure 5 also shows the derived piston velocity. This is a linear piecewise function.

For the projectile, the velocity has been recorded using radar. However, this trace is normally accurate only for the middle part of the travel, where the slope of the velocity is fairly constant. To obtain the projectile travel, I fit this section of the curve with two parabolas (see Figure 6). The knot point is where the chamber pressure reaches its maximum. I can then extrapolate in both directions. The projectile travel is now easily obtained by numerical integration.

The projectile has a nominal shot start pressure of 68 MPa. Extrapolating the projectile travel back to zero, I normally obtain a value of shot start pressure between 65 and 70 MPa.

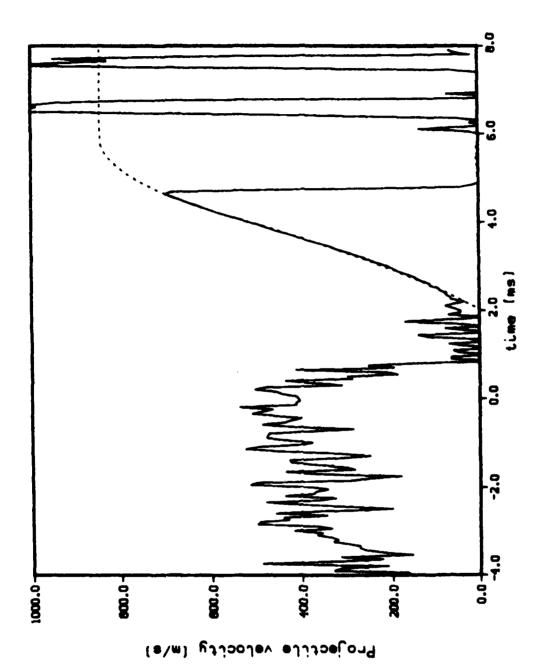
The projectile is seated in the gun tube by hammering. Looking at the raw interferometer data, the projectile seems to move slightly before it is firmly lodged in place. The experimental data is not detailed enough to determine this quantitatively. So I assume that the projectile does not move at all until the pressure reaches 68 MPa.

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For Round 8, the gun tube pressures were not recorded. So I also consider Round 53. In this case, the liquid pressure was not successfully recorded, so it is approximated as the chamber pressure times the hydraulic difference. Figure 7 compares the chamber pressures for the two rounds. For Round 53, the spray appears to ignite more rapidly. Also, the behavior near the maximum pressure is quite different. The shape of the pressure curve for Round 8 is more typical.

#### VI. DATA ANALYSIS

In the gun code, the mass flux through the piston is assumed to obey the steady state Bernoulli law



Projectile Velocity; Round 8; Measured (line) and Derived (dot) Figure 6.

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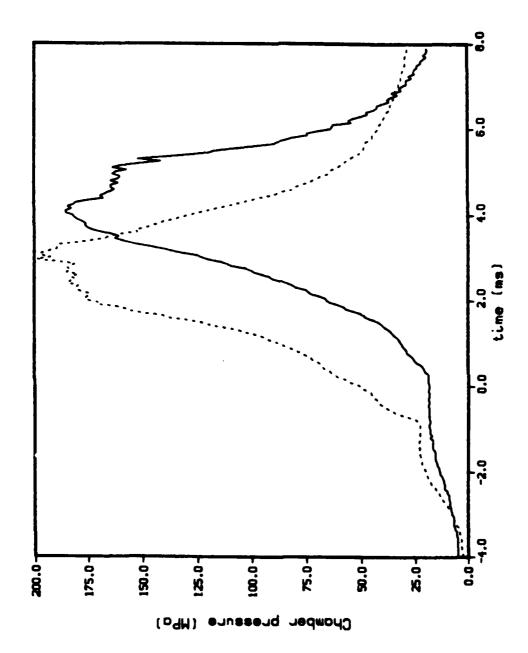


Figure 7. Chamber pressure; Round 8 (line) and Round 53 (dot)

mass flux = 
$$C_D A_v \sqrt{2g_0} \rho_1 (p_1 - p_3)$$
 (3)

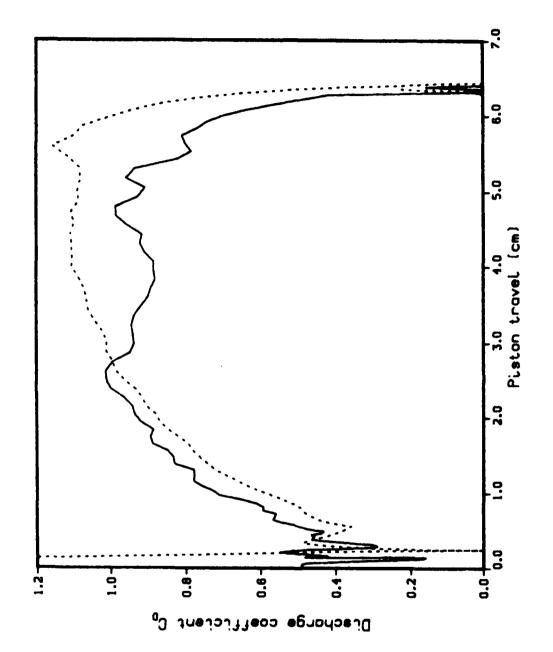
where  $C_D$  is the discharge coefficient,  $A_v$  is the vent area,  $g_o$  is a conversion constant,  $\rho_1$  is the liquid density,  $p_1$  is the liquid pressure, and  $p_3$  is the combustion chamber pressure.

From the experiment, the pressures and vent area are known. The liquid density can be computed from the equation of state, and the liquid mass in the reservoir is just density times volume. The liquid reservoir mass is fit by cubic splines. The time derivative of this mass can then be taken analytically, and equals the mass flux into the combustion chamber. The discharge coefficient can now be determined.

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Results are given in Figure 8. The values are plotted versus the piston travel to make comparisons easier. The early noise is due to the liquid pressure oscillations from the Belleville springs. The discharge coefficient then increases relatively slowly to a more or less steady value. For Round 53, the discharge coefficient becomes larger. This is due to the differences in the chamber pressures for the two rounds. The curves are similar to the results in the previous BRL report. The changes are due to a more accurate accounting for the motion of the Belleville springs and the more accurate method for approximating time derivatives. Because the problem is transient, the discharge coefficient may be greater than one.

It is also possible to compute the liquid accumulation, using conservation of mass and energy. At any given time, we know how much liquid is still in the reservoir. The balance of the original charge is in the combustion chamber/gun tube. We assume that when the liquid combusts, it immediately releases all of its chemical energy. The total energy in the system must equal the chemical energy in the liquid, the internal energy in the gas, and the kinetic energy of the piston, the projectile, and the gas. Energy loss terms (heat loss to the tube, air shock, frictional resistance, etc.) are ignored.



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Figure 8. Discharge Coefficient into Combustion Chamber;
Round 8 (line) and Round 53 (dot)

The tube pressure is assumed to satisfy a habitance pressure distribution. The throat pressure is set equal to the pressure at the first gun tube pressure transducer (3.81 cm from the throat). If the gun tube pressure has not been recorded, I use the chamber pressure.

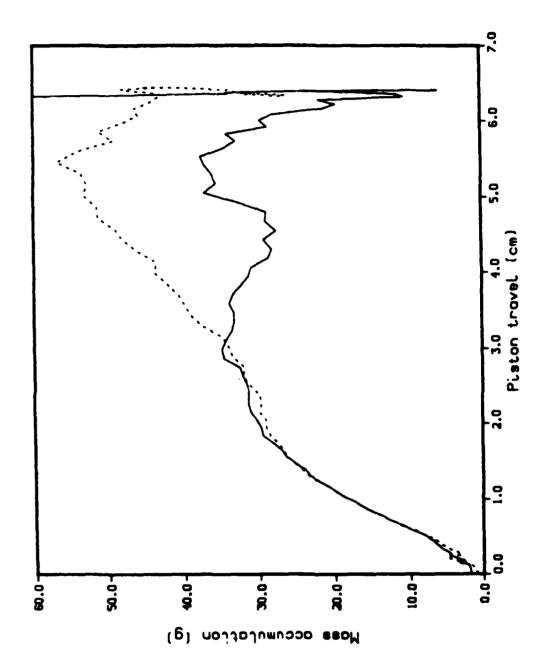
From the piston travel and projectile travel, the volumes of the combustion chamber and the gun tube are computed. Also, the kinetic energy of the piston, the kinetic energy of the projectile, and the kinetic energy of the fluid in the tube (assuming a Lagrange distribution) can be calculated. The liquid density can be calculated from the equation of state.

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We can now set up eleven equations involving the combustion chamber/gun tube; total energy, total mass, volume of chamber and tube, internal energy of the gas (Noble-Abel equation) for chamber and tube, liquid density for chamber and tube, gas density for chamber and tube, and average tube pressure. Unfortunately, there are thirteen unknowns; liquid mass, gas mass, liquid volume, gas volume, gas density, and gas internal energy for both chamber and gun tube, and average tube pressure. Additional assumptions are necessary. I assume that the liquid is evenly distributed in the chamber/tube, and that the internal energy of the gas is the same in the chamber and the gun tube. Details of the equations are in Appendix A.

Results are given in Figure 9. There is a significant liquid accumulation, and large amounts of liquid remain until late in the firing cycle. The results should be accurate at early times. Round 53 shows larger accumulation because the gun tube pressure has been recorded. This pressure is less than the chamber pressure, which I am using for Round 8, and so the gun tube gas has less energy. The above analysis ignores any loss terms (such as heat loss to the gun tube walls), and assumes that the fluid in the combustion chamber is stagnant (no kinetic energy). So there is either significant liquid accumulation, or there are important loss terms not usually taken into account.

One possible source of error is the water purge of the system. Before the liquid reservoir is filled and prepressurized, the system is purged with water. This may contaminate the propellant. For a similar GE test fixture,



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Figure 9. Mass Accumulation in the Combustion Chamber/ Gun Tube; Round 8 (line) and Round 53 (dot)

the liquid in the reservoir is estimated to be as much as 5% water (by volume).  $^{13}$ 

To check on the possible effect of water contamination, I also ran the code assuming 5% water. This was done by changing the initial density of the fluid and its chemical energy. Results are shown in Figure 10. The change is relatively minor.

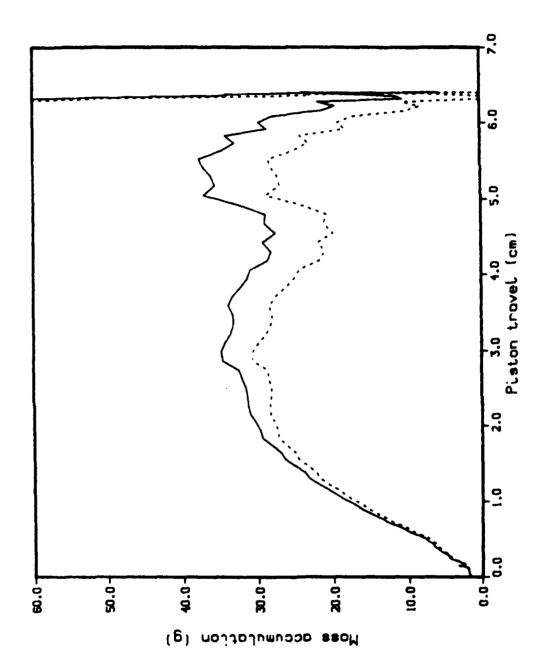
Heat loss has also been ignored in the above analysis. In gun codes, a heat loss of 5% of the total energy of the system is typical, primarily occurring in the gun tube. This level of heat loss would give results similar to the assumption of 5% water contamination.

Additional information can be obtained concerning the burning rate. Assume that the liquid accumulation is in the form of uniform size droplets. The diameter  $\mathbf{d}_S$  of the droplets is chosen to be the Sauter mean diameter. This is the diameter that preserves the surface area of the original accumulation. Then

burning rate = 
$$M_{L3}$$
 (6/d<sub>S</sub>)  $Ap_3^B + M_{L4}$  (6/d<sub>S</sub>)  $Ap_4^B$  (4)

where  ${\rm M_{L3}}$  is the liquid in the chamber and  ${\rm M_{L4}}$  is the liquid in the tube. The burning rate is equal to the rate of change of the mass of the gas. Again fitting the total gas mass by splines, the Sauter mean diameter can be calculated (see Figure 11). For early times, the diameter is large, indicating rapid liquid accumulation and slow burning. The diameter then drops rapidly, indicating that the liquid is burning much more efficiently. The liquid accumulation still remains high, but this is due to the rapid influx of propellant from the liquid reservoir. The drop diameter increases late in the cycle. This may actually reflect less efficient combustion, or it may just reflect inaccuracies in the burning rate.

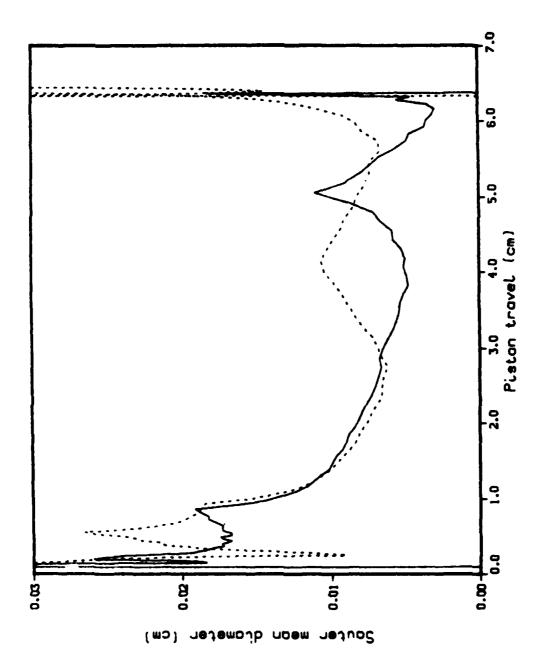
Finally, the mass flux into the gun tube is assumed to be isentropic flow.



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Figure 10. Mass Accumulation in the Combustion Chamber/Gun Tube; Round 8; Pure Propellant (line) and with 5% Water (dot)



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Figure 11. Sauter Mean Diameter of the Liquid Accumulation; Round 8 (line) and Round 53 (dot)

mass flux =

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$$c_{T}^{A_{4}\rho_{3}} \neq 2g_{o} \{b(p_{3} - p_{th}) + c_{p}^{T}_{th}(p_{3}/p_{4})^{(\gamma-1)/\gamma} - 1\}\}$$
 (5)

where  $C_T$  is the discharge coefficient,  $A_4$  is the area of the gun tube, b is the covolume of the gas,  $c_p$  is the specific heat of the gas,  $T_{th}$  is the temperature in the gun tube throat, and  $\gamma$  is the ratio of specific heats. The mass flux is the rate of change of the mass in the tube. So  $C_T$  can be computed, and is shown in Figure 12. This result is less accurate than the previous discharge coefficient, since the pressure difference between the chamber and the gun tube is relatively small. If Bernoulli flow is assumed instead of isentropic flow, the results are similar.

#### VII. COMPARISONS

Now we will see what effect the above results have on our use of the gun code. First the code<sup>5</sup> is run with the usual assumptions. That is, the discharge coefficient is constant with respect to time and the value is chosen to match the desired chamber pressure. The liquid is assumed to burn instantaneously upon entering the combustion chamber (zero liquid accumulation). The discharge coefficient into the gun tube is one. A simple model for air shock and heat loss to the gun tube is included. The pressure distribution in the gun tube is approximated by a modified Lagrange distribution, which takes into account the non-zero fluid velocity at the throat of the tube.

Next, the code is run using the experimental values derived above (for Round 8). The discharge coefficient into the gun tube is read in as a function of piston travel. The liquid injected into the combustion chamber is assumed to form droplets. All the droplets have the same diameter, but this varies with piston travel. Since Round 53 was somewhat different from Round 8, the discharge coefficient into the gun tube will be considered separately. This was only computed for Round 53, and is considered to be less accurate than the other two parameters. For the runs below, this discharge coefficient

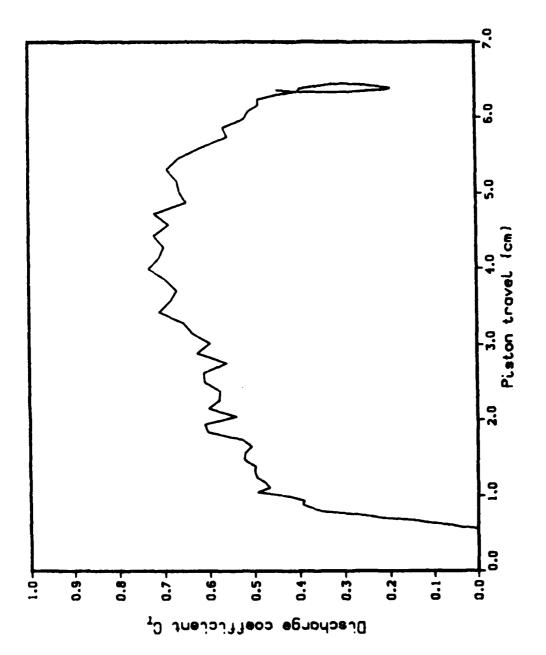


Figure 12. Discharge Coefficient into Gun Tube; Round 53

is set uniformly equal to one. For the purposes of comparison, all the graphs are translated in the time direction so that the chamber pressures reach the shot start pressure (68 MPa) at the same time.

The results for chamber pressure are given in Figure 13. The model using the experimental values reproduces the shape of the pressure curve reasonably well. It it less accurate at early times, since there is no Belleville spring model or primer combustion model in the gun code. It is also less accurate at very late times, when the inverse code is less accurate. The maximum chamber pressure is slightly off, but there was no attempt made to vary the parameters to match this pressure. The simpler model shows a much more rapid pressure rise.

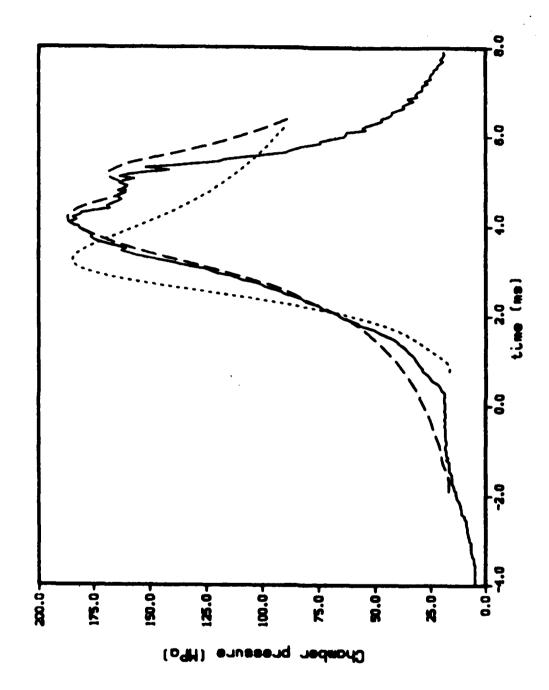
Figure 14 shows the piston travel. The simpler model shows the piston moving slower, since the chamber pressure falls off earlier. In fact, the projectile exits the muzzle before all the liquid is injected.

The projectile velocity is given in Figure 15. The more complicated model shows reasonable agreement.

Figure 16 and 17 show the gun tube pressures. The models give a pressure rise that is later in time than the experimental results. In the models, a shot start pressure of 68 MPa is assumed. This appears to be a good estimate, but in practice the projectile moves a short distance before it is seated firmly. The experimental data indicates that the projectile is already at the first pressure transducer (3.81 cm downbore) when the pressure reaches 68 MPa.

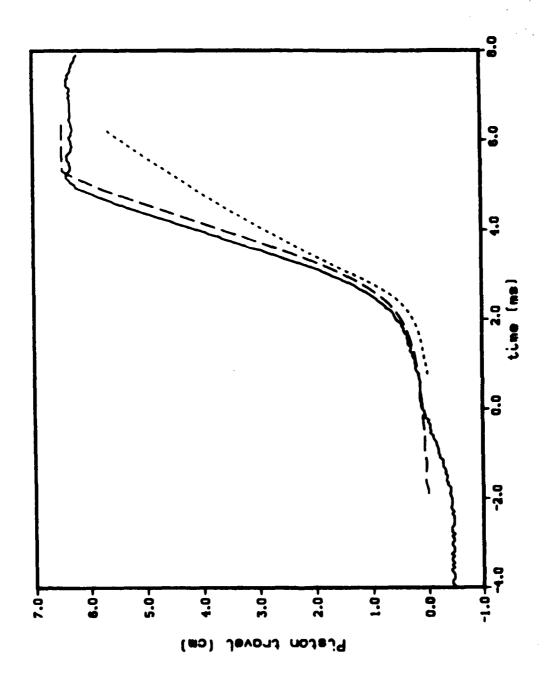
The muzzle velocity for the first model is 1010 m/s and for the second is 1099 m/s. The experimental muzzle velocity is between 1000 and 1020 m/s. The higher velocity for the more complicated model reflects the higher chamber pressure. Also, there are probably additional loss terms not included in the model.

I ran the gun code adding the experimental values for the discharge coefficient into the gun tube (Round 53). The only noticeable result was that the maximum chamber pressure rose 12 MPa. The gun tube pressures and



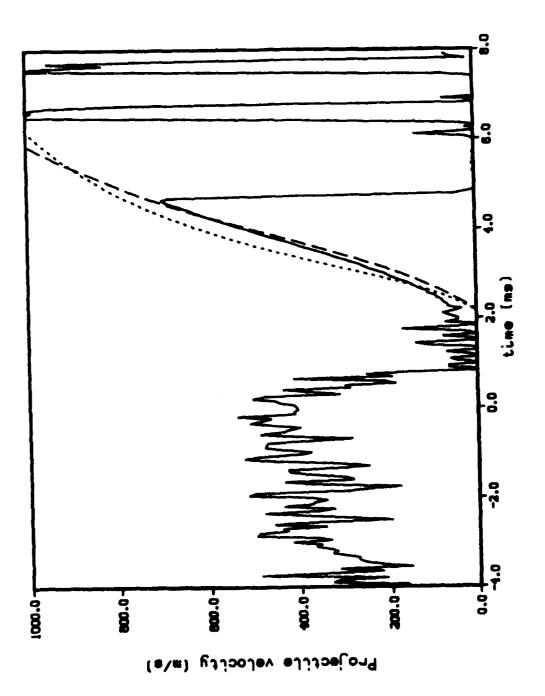
Model - Cn=0.59 and Instantaneous Cn and de from Round 8 (dash) Figure 13. Chamber Pressure for Round 8 (line).

burning (dot). Model - C, and d burning (dot).



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Piston Travel for Round 8 (line). Model - Cp=0.59 and Instantaneous burning (dot). Model - Cp and dg from Round 8 (dash) Figure 14.



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8 (line). Model - Cp=0.59 and Instantaneous Cp and dg from Round 8 (dash) Projectile Velocity for Round 8 (line).

burning (dot). Model - Cp and d Figure 15.

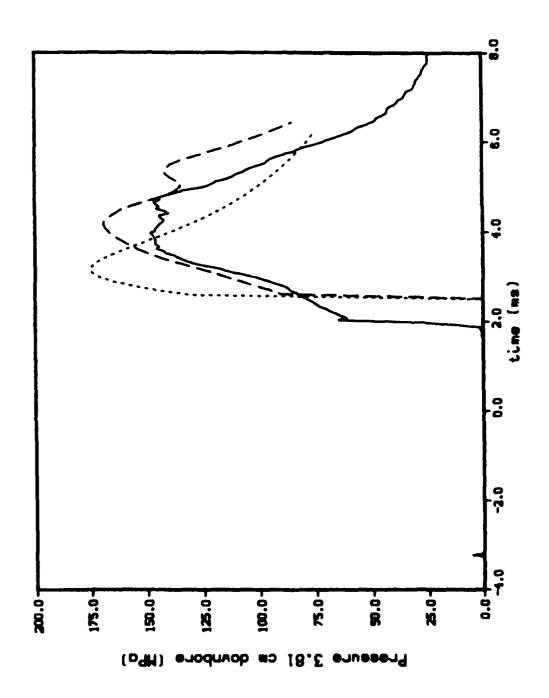
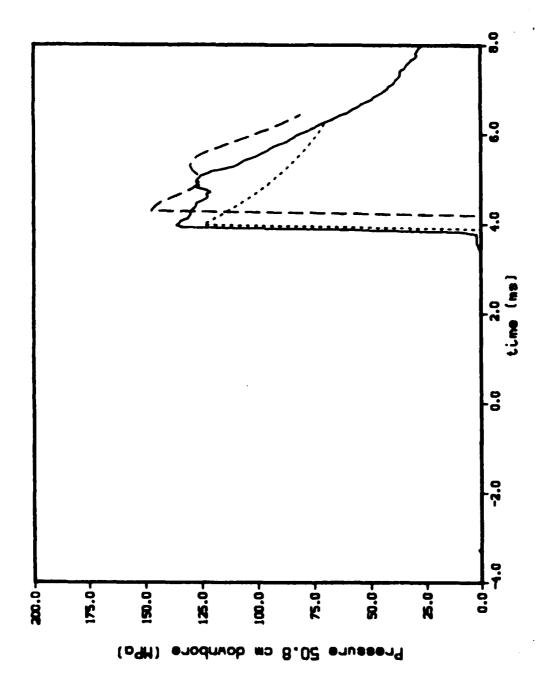


Figure 16. Gun Tube Pressure (3.81 cm Downbore) for Round 53 (line). Model - Cp=0.59 and Instantaneous burning (dot). Model - Cp and dg from Round 8 (dash)



Round 53 (line). Model - Cp=0.59 and - Cp and ds from Round 8 (dash) Gun Tube Pressure (50.8 cm Downbore) for Round 53 (line). Instantaneous burning (dot). Model - Cp and dg from Figure 17.

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projectile velocity were practically unchanged. The injection into the gun tube seems to be controlled primarily by the projectile motion. If a smaller discharge coefficient is chosen, the chamber pressure increases sufficiently to sustain about the same injection rate.

In addition, I ran the gun code using the values derived from Round 53 instead of Round 8. The results were qualitatively very similar. The predicted chamber pressure fell 15 MPa, and the second peak in the chamber pressure curve was flattened out. The predicted muzzle velocity decreased by 28 m/s.

#### VIII. TRANSIENT INJECTION MODELS

It seems reasonable to try to explain the discharge coefficients as due to transient behavior. This involves setting up an unsteady equation for the mass flux.

I assume that the flow in the liquid reservoir is isothermal. In conservation form, the quasi two-dimensional mass and momentum equations are

$$\frac{\partial(\rho A)}{\partial t} = -\frac{\partial}{\partial x} (\rho v A) \tag{6}$$

$$\frac{\partial(\rho v A)}{\partial t} = -\frac{\partial}{\partial x} (\rho v^2 A) - g_0 A \frac{\partial p}{\partial x}$$
 (7)

where v is the liquid velocity and A is the cross sectional area. The coordinate system is fixed with respect to the piston. This is convenient since the division between the liquid reservoir and the combustion chamber is defined by the front corner of the piston. I want to approximate the momentum equation while retaining the simple lumped parameter model.

The assumption I make is that the space derivative of the mass flux pvA is zero. From the experimental data, this gradient is in fact quite small. Then taking the momentum equation, and integrating from the back wall of the liquid reservoir to the orifice exit, one obtains

$$\frac{\partial(\rho vA)}{\partial t} = [0.5 \ \rho_1 \ (v_{ps}^2 - v_3^2) + g_0(p_1 - p_3)] / \int dx/A$$
 (8)

where  $\mathbf{v}_{ps}$  is the piston velocity and  $\mathbf{v}_3$  is the injection velocity of the fluid. The integral of the inverse of the area is approximated assuming a slightly simplified piston shape.

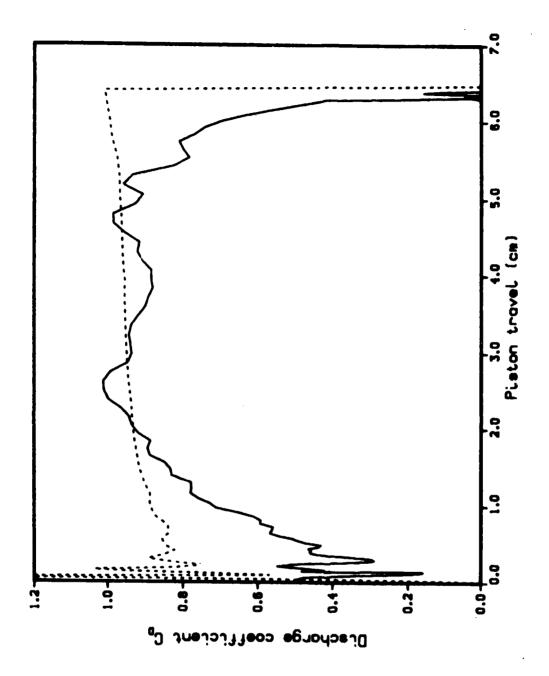
The above form ignores loss terms. To take this into effect, I multiply the pressure term by a constant discharge coefficient squared.

I implemented this model into the gun code, and ran the code using the experimentally derived Sauter mean diameters and the new transient mass flux model ( $C_{\rm D}$  = 0.958). Given the resulting mass flux, corresponding steady state discharge coefficients can be derived. Figure 18 shows the comparison with the experimental discharge coefficients. While the new model shows the qualitative behavior of a time delay in the rise to steady state discharge coefficients, the rise time is much too rapid.

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The difficulty follows from the form of the equations. At the beginning, the mass flux is well below steady state values. Since the liquid cannot be injected through the piston, it is compressed, leading to a rapid pressure rise. But a relatively small pressure difference leads to a very large increase in the mass flux time derivative. Because of this feedback with the piston motion, the approach to steady state is very rapid.

Work is now going on with higher dimensional models to try to understand this procedure better.



Transient Model Discharge Coefficient into Combustion Chamber; Round 8 (line). Discharge Coefficient into Combustion Chamber (dot) Figure 18.

### IX. CONCLUSIONS

We have demonstrated the change in the discharge coefficient during the firing cycle and the accumulation of liquid in the combustion chamber. Both of these effects are important in resolving the details of the firing cycle. But if the proper maximum chamber pressure is achieved, the effect on muzzle velocity is relatively minor.

Attempts have been made to predict the injection into the combustion chamber, instead of using experimentally derived values. While the behavior can be qualitatively predicted, the quantitative behavior cannot be reproduced.

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# LIST OF SYMBOLS

<b>A</b> <sub>1</sub>	area of liquid reservoir, cm <sup>2</sup>
A <sub>3</sub>	area of combustion chamber, cm <sup>2</sup>
A <sub>4</sub>	area of the gun tube, $cm^2$ .
Ag	area of the grease dyke, cm <sup>2</sup>
A <sub>h</sub>	area of the piston hole, $cm^2$
A <sub>v</sub>	vent area between piston and bolt, cm <sup>2</sup>
Ъ	covolume of the gas, cm <sup>3</sup> /g
c <sub>v</sub>	specific heat at constant volume, joules/g-K
c <sub>p</sub>	specific heat at constant pressure, joules/g-K
$c_{\mathbf{D}}$	discharge coefficient into the combustion chamber
$c_{\mathbf{r}}$	discharge coefficient into the gun tube
<sup>d</sup> s	Sauter mean diameter for the droplet distribution, cm
E <sub>K4</sub>	kinetic energy of the fluid in the tube, joules
E <sub>34</sub>	total energy in the combustion chamber/gun tube, joules
E <sub>ps</sub>	kinetic energy of the piston, joules
<sup>E</sup> pj	kinetic energy of the projectile, joules
Et	total energy in the gun system, joules
e <sub>1</sub>	chemical energy of the liquid, joules/g
e <sub>3</sub>	internal energy of the gas in the chamber, joules/g
e <sub>4</sub>	
	internal energy of the gas in the tube, joules/g
g <sub>o</sub>	internal energy of the gas in the tube, joules/g conversion constant, $10^7 \text{ g/s}^2$ -cm-MPa
g <sub>o</sub> K <sub>l</sub>	
	conversion constant, $10^7 \text{ g/s}^2$ -cm-MPa
κ <sub>1</sub>	conversion constant, $10^7 \text{ g/s}^2$ -cm-MPa bulk modulus of the liquid at zero pressure, MPa
κ <sub>1</sub> κ <sub>2</sub>	conversion constant, $10^7 \text{ g/s}^2$ -cm-MPa bulk modulus of the liquid at zero pressure, MPa derivative of the bulk modulus

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mass of the liquid in the gun tube, g
M<sub>L4</sub>
           mass of the gas in the gun tube, g
M_{G4}
            total mass in the gun tube, g
M<sub>4</sub>
            mass of the liquid in the combustion chamber/gun tube, g
M<sub>1.34</sub>
           mass of the gas in the combustion chamber/gun tube, g
M<sub>G34</sub>
            total mass in the combustion chamber/gun tube, g
M<sub>34</sub>
            mass of the piston, g
Mps
            mass of the projectile, g
Mpj
            pressure in the liquid reservoir, MPa
Pį
            pressure in the combustion chamber, MPa
P3
            average pressure in the gun tube, MPa
P4
            pressure at the gun tube throat, MPa
P_{th}
            maximum piston travel, cm
Smax
T3
            temperature in the combustion chamber, K
            average temperature in the gun tube, K
T
            temperature at the gun tube throat, K
Tth
            volume of the liquid reservoir, cm<sup>3</sup>
\mathbf{v}_1
            volume of the combustion chamber, cm<sup>3</sup>
N<sup>3</sup>
            volume of the liquid in the combustion chamber, cm3
v_{L3}
            volume of the gas in the combustion chamber, cm3
v_{G3}
            volume of the gun tube, cm<sup>3</sup>
٧
            volume of the liquid in the gun tube, cm<sup>3</sup>
V<sub>L4</sub>
            volume of the gas in the gun tube, cm<sup>3</sup>
V_{G4}
            volume of the liquid in the combustion chamber/gun tube, cm3
V<sub>L34</sub>
            volume of the gas in the combustion chamber/gun tube, cm3
V<sub>G34</sub>
            total volume of the combustion chamber/gun tube, cm3
V<sub>34</sub>
            velocity of the piston, cm/s
v<sub>ps</sub>
```

<sup>v</sup> pj	velocity of the projectile, cm/s					
<b>v</b> <sub>3</sub>	injection velocity of the fluid into the chamber, cm/s					
Υ	ratio of specific heats					
<sup>р</sup> o	density of the liquid at atmospheric pressure, $g/cm^3$					
ρl	density of the liquid in the reservoir, $g/cm^3$					
ρ <sub>L3</sub>	density of the liquid in the combustion chamber, $g/cm^3$					
ρ <sub>G3</sub>	density of the gas in the combustion chamber, $g/cm^3$					
ρ <sub>L4</sub>	density of the liquid in the gun tube, $g/cm^3$					
р <sub>С</sub> 4	density of the gas in the gun tube, $g/cm^3$					

APPENDIX A

#### APPENDIX A

The properties of the fluid in the combustion chamber/gun tube are found using conservation of mass and energy. At any given time, the mass of the liquid remaining in the reservoir is known. Assuming the reservoir liquid is isothermal, we also know its chemical energy. Our basic assumption is that the system is adiabatic. That is, all loss terms are ignored (such as heat loss to the gun tube). So we can compute the total mass and energy of the combustion chamber/gun tube. A secondary assumption is that the liquid combusts completely. That is, when the liquid burns, it turns immediately into final products and releases all its chemical energy.

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The set of equations is total energy:

$$E_{34} = e_1 (M_{L3} + M_{L4}) + e_3 M_{G3} + e_4 M_{G4}$$
 (A1)

total mass:

$$M_{34} = M_{L3} + M_{G3} + M_{L4} + M_{G4}$$
 (A2)

volumes:

$$v_3 = v_{L3} + v_{G3} \tag{A3}$$

$$V_4 = V_{L4} + V_{G4} \tag{A4}$$

internal energy (Noble-Able equation):

$$e_3 = c_v T_3 = p_3 (1 - b \rho_{G3})/[\rho_{G3} (\gamma - 1)]$$
 (A5)

$$e_4 = c_v T_4 = p_4 (1-b \rho_{G4})/[\rho_{G4}(\gamma - 1)]$$
 (A6)

average gun tube pressure (Lagrange distribution):

$$p_4 = p_{th} [1 + M_4/(3M_{pj})]/[1 + M_4/(2M_{pj})]$$
 (A7)

and densities:

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$$\rho_{L3} = M_{L3}/V_{L3} \tag{A8}$$

$$\rho_{G3} = M_{G3}/V_{G3} \tag{A9}$$

$$\rho_{L4} = M_{L4}/V_{L4} \tag{A10}$$

$$\rho_{G4} = M_{G4}/V_{G4} \tag{A11}$$

The thirteen unknowns are  $p_4$ ,  $M_{L3}$ ,  $M_{G3}$ ,  $M_{L4}$ ,  $M_{G4}$ ,  $V_{L3}$ ,  $V_{G3}$ ,  $V_{L4}$ ,  $V_{G4}$ ,  $\rho_{L3}$ ,  $\rho_{G3}$ ,  $\rho_{L4}$ , and  $\rho_{C4}$ . To solve the equations, I assume that the liquid is evenly distributed in the combustion chamber/gun tube, that is:

$$M_{L4} = M_{L3} V_4 / V_3$$
 (A12)

Finally, I assume that the internal energy of the gas is the same in the combustion chamber and the gun tube, that is:

$$e_3 = e_4 \tag{A13}$$

Since the specific heat is taken to be constant, this means that the temperature is the same. This is consistent with Bernoulli flow, but not with isentropic flow. However, in running the gun code, the temperature difference between the combustion chamber and the throat is usually no larger than 100K. Until temperature measurements are made, this is the best assumption that I can make.

The above equations are actually solved using an iterative procedure. To start with, the mass terms are estimated. The total mass  $M_{34}$  is known. I assume that the fraction of the total mass for each mass term is the same as for the previous time step. For time zero, there is no liquid accumulation, so the starting point is easily calculated. Then the following equations are solved in the given order.

Kinetic energy of the gas in the gun tube (Lagrange distribution):

$$E_{K4} = 0.5 M_4 v_{pj}^2 / 3g_o$$
 (A14)

total energy in the combustion chamber/gun tube:

$$E_{34} = E_t - e_1 M_1 - E_{ps} - E_{pi} - E_{K4}$$
 (A15)

internal energy of the gas

$$e_3 = e_4 = [E_{34} - e_1 M_{134}] / M_{G34}$$
 (A16)

average gun tube pressure

$$p_4 = p_{th} [1 + M_4/3 M_{pj}] / [1 + M_4/2 M_{pj}]$$
 (A17)

average gun tube liquid density:

$$\rho_{L4} = \rho_0 \left[ -\frac{\kappa_2}{\kappa_1} p_4 + 1 \right]^{1/\kappa_2}$$
 (A18)

gas densities:

$$\rho_{G3} = \rho_3/[e_3 (\gamma - 1) + \rho_3 b]$$
 (A19)

$$p_{G4} = p_4/[e_4 (\gamma - 1) + p_4 b]$$
 (A20)

volumes:

$$V_{L3} = M_{L3}/\rho_{L3} \tag{A21}$$

$$V_{L4} = M_{L4}/\rho_{L4}$$
 (A22)

$$v_{G3} = v_3 - v_{L3}$$
 (A23)

$$V_{G4} = V_4 - V_{L4}$$
 (A24)

and finally new values for the masses:

$$^{\mathsf{M}}_{\mathsf{G3}} = ^{\mathsf{p}}_{\mathsf{G3}} ^{\mathsf{V}}_{\mathsf{G3}}$$
 (A25)

$$^{\mathsf{M}}_{\mathsf{G4}} = ^{\mathsf{p}}_{\mathsf{G4}} \, ^{\mathsf{V}}_{\mathsf{G4}} \tag{A26}$$

$$M_{L3} = M_{L34} V_3 / V_{34}$$
 (A27)

$$M_{L4} = M_{L34} V_4 / V_{34}$$
 (A28)

The process is repeated until convergence is obtained. Since for any time step only minor changes occur, this has not been observed to take more than a maximum of twenty iterations. After going through all the data points in order, all the quantities needed to compute the mass accumulation and the discharge coefficient into the gun tube are available.

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